



Thickness dependence of critical Currents in CC: microstructure or pinning size effects?

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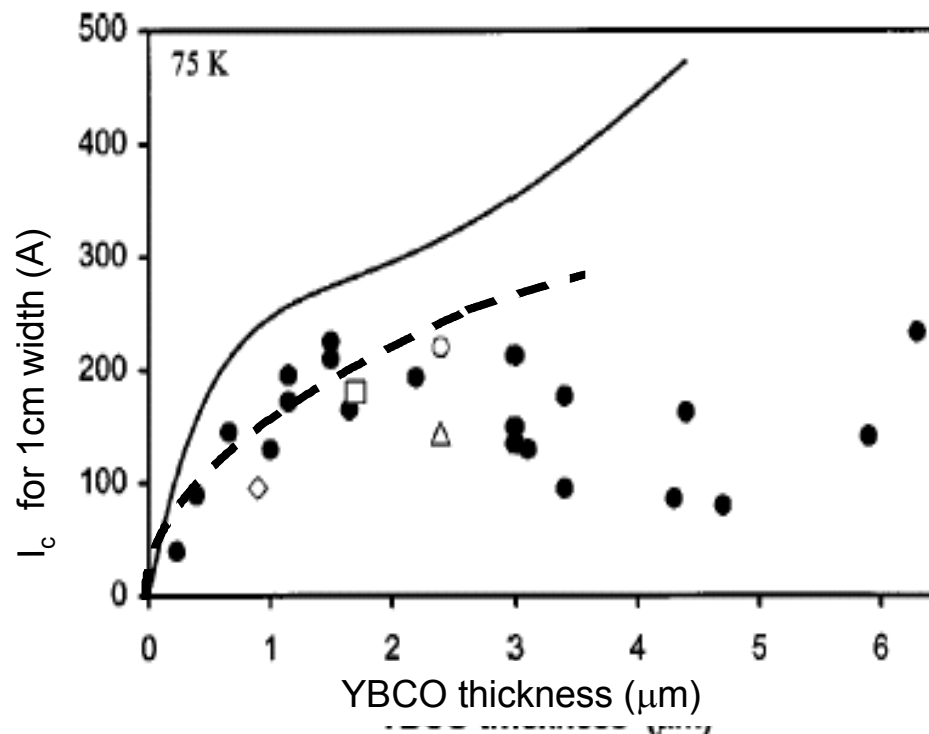
St. Petersburg, FL, Jan 21, 2003



MOTIVATION

S. Foltyn et al.

- Can pinning provide mechanisms resulting in the observed dependence $J_c(d)$
- Additional pinning centers, dead layers or **size effects?**
- Different mechanisms for zero-field and in-field J_c
- Self-field limitations
- 2D-3D dimensional crossover in single-vortex and collective pinning

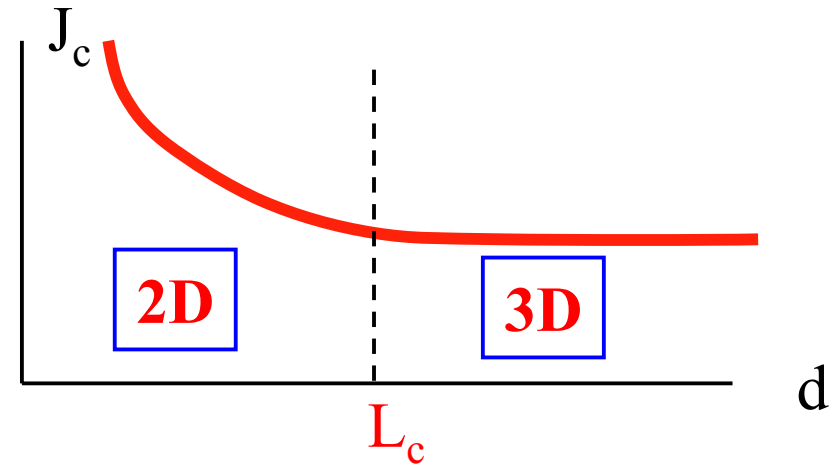
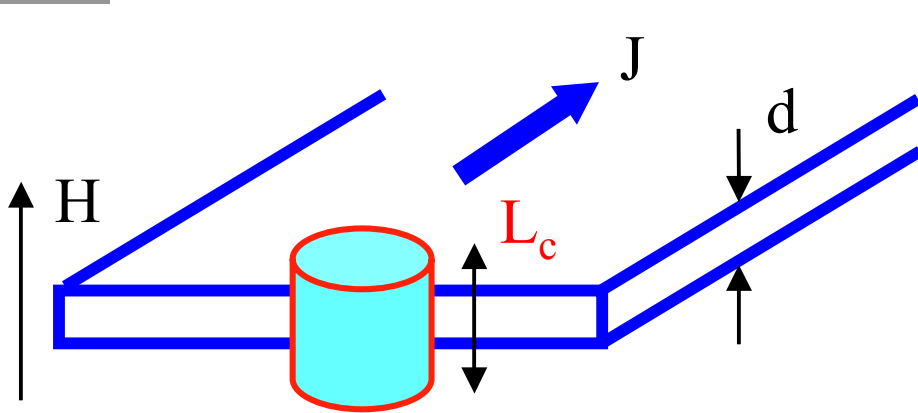


Add more YBCO, but I_c does not increase.

$$I_c \propto \sqrt{d} \quad (\text{low fields})$$

$$I_c \propto \text{const} \quad (\text{high fields})$$

SIZE EFFECT IN COLLECTIVE PINNING



- 3D-2D pinning transition if $d < 2L_c$: $L_c \rightarrow d$
- High-field thickness dependence (Kes and Tsuei, Brandt):

$$J_c \cong n_p U_p^2 / Br_p c_{66} d \propto 1/d, \quad I_c(d) = \text{const}$$

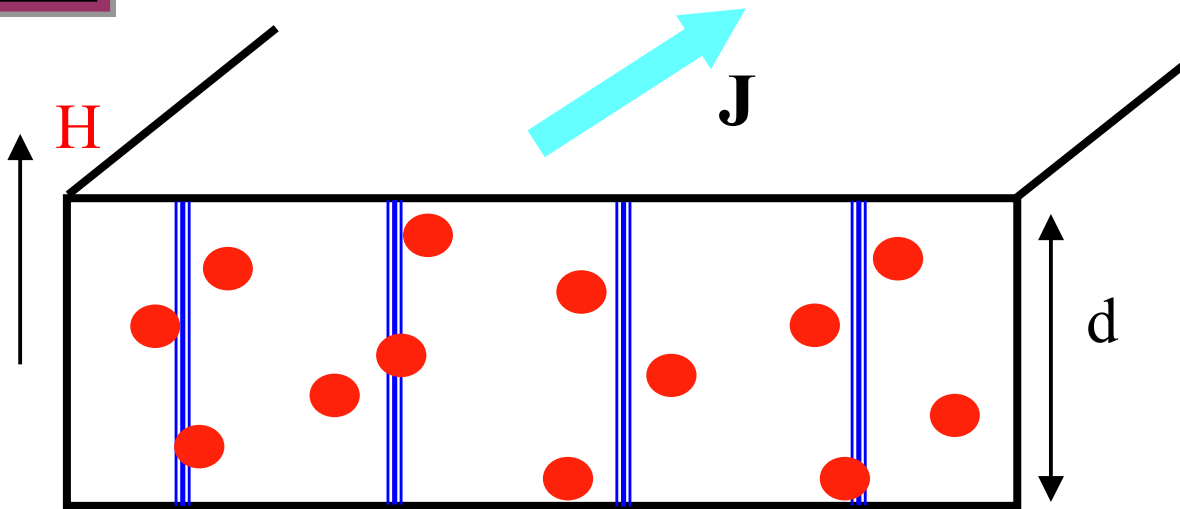
- Dimensional crossover in collective pinning (Wordenweber & Kes, 1986)

$$d[\mu\text{m}] < d_c \approx 2B^{1/4}[\text{Tesla}] / \sqrt{J_c}[\text{MA/cm}^2]$$

For $B = 1\text{T}$, and $J_c = 1\text{MA/cm}^2$, this yields $d_c \approx 2\mu\text{m}$



SINGLE-VORTEX PINNING IN A FILM



- Rigid infinite vortex in a random potential: **PINNING FORCE = 0**
- Rigid finite vortex in a film: pinning force is **FINITE**.

$$\phi_0 J_c d \cong \frac{f_p}{\sqrt{N}} \times \frac{r_0}{l_i} \times N$$

$$J_c \cong \frac{U_p}{\phi_0} \sqrt{\frac{n_p}{d}}$$

$N = d/l_i$ is the number of pins per vortex, l_i is the pin spacing, $n_p = l_i^{-3}$, $U_p = f_p r_0$ is the pinning energy



Effect of thermal fluctuations

Fluctuating vortex in a pinning potential

$$\eta \dot{x} = \phi_0 J - \phi_0 J_c(d) \sin kx + \zeta(t) / d$$

Same Eq. as for a Josephson Junction gives the exact E-J characteristics (Ambegaokar & Halperin, 1968)

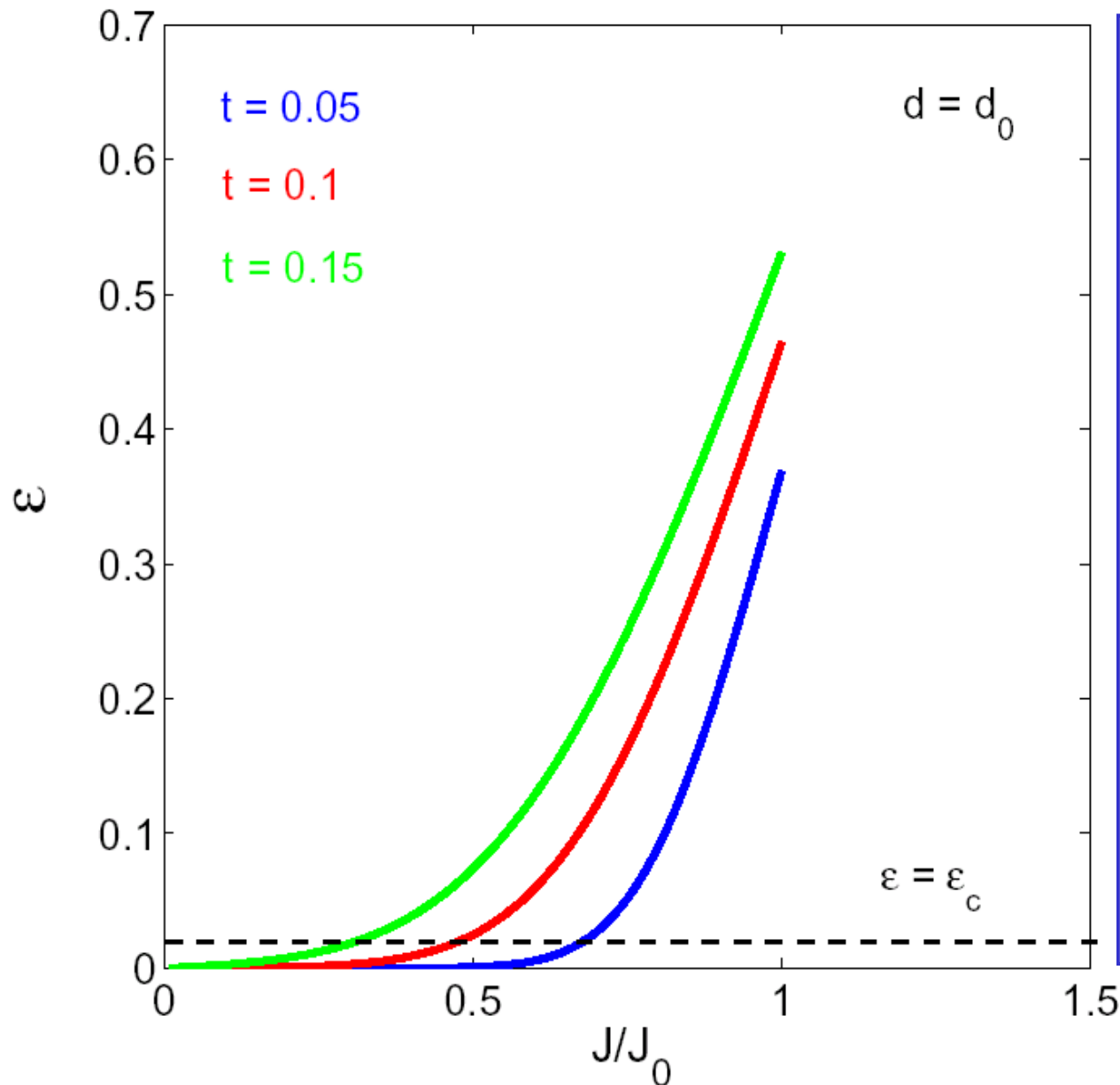
$$\varepsilon = t(1 - e^{-\pi\beta\alpha/t}) / \alpha D, \quad D = \int_0^\pi e^{-\pi\beta\alpha\theta/t} I_0 \left(\frac{\sqrt{\alpha}}{t} \sin \theta \right) d\theta$$

Dimensionless parameters

$$\varepsilon = \frac{E}{\rho_F J_0}, \quad \alpha = \frac{d}{d_0}, \quad \beta = \frac{J}{J_0}, \quad J_c = J_0 \sqrt{\frac{d_0}{d}}, \quad t = \frac{\pi k_B T}{J_0 \phi_0 d_0 r_p}$$



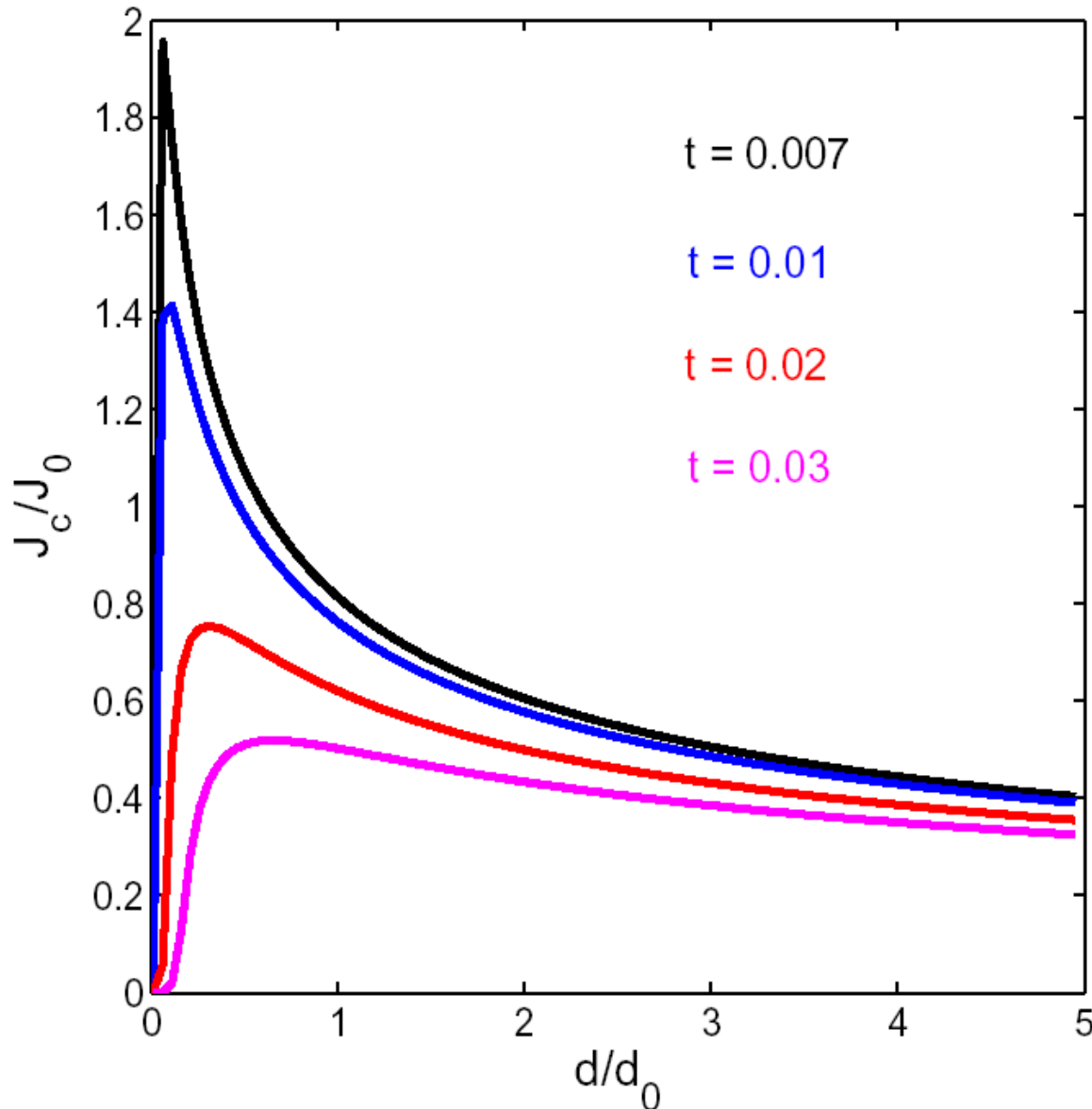
Current-voltage characteristics



- Exact $E(J)$ as a function of T, H and d
- Thermal fluctuations broaden $E(J)$ and reduce J_c
- Define $J_c(d)$ at a given electric field criterion
- $\varepsilon_c = E_c / \rho_F J_0 = 10^{-5}$ for $J_0 = 1 \text{ MA/cm}^2$, $E_c = 1 \text{ } \mu\text{V/cm}$, and $\rho_F = 10 \text{ } \mu\Omega\text{cm}$



Thickness dependence of J_c



- Effective temperature:

$$t = \frac{\pi k_B T}{\phi_0 J_0(T, H) d_0 r_p(T)}$$

- Maximum at $d = d_m$ due to competition between pinning and thermal fluctuations
- As T and H increase, d_m **increases**
- Reveal the peak in $J_c(d)$ at higher H and T

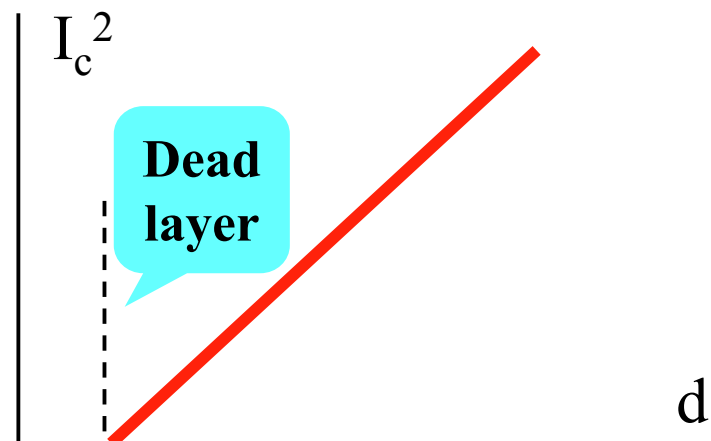


Conclusions

Low T and H

Distinctive features of the 2D pinning:

1. Square-root dependence of $I_c(d)$ at low H
2. Maximum in $J_c(d)$ at higher T and H
3. The maximum in $J_c(d)$ at higher T and H distinguishes the pinning size effects from microstructural factors (dead layers, etc).



High T and H

